

- 1.) A laser emits light of frequency $4.74 \times 10^{14} \text{ sec}^{-1}$. What is the wavelength of the light in nm?

$$\lambda = \frac{c}{\nu} = \frac{2.998 \times 10^8 \text{ m}}{\text{s}} \times \frac{1 \text{ s}}{4.74 \times 10^{14}} \times \frac{1 \text{ nm}}{10^{-9} \text{ m}} = \boxed{6.32 \times 10^2 \text{ nm}}$$

- 2.) A certain electromagnetic wave has a wavelength of 625 nm.

- a.) What is the frequency of the wave?

$$\nu = \frac{c}{\lambda} = \frac{2.998 \times 10^8 \text{ m/s}}{6.25 \times 10^{-7} \text{ m}} \quad \frac{625 \text{ nm} \times \frac{10^{-9} \text{ m}}{1 \text{ nm}} = 6.25 \times 10^{-7} \text{ m}}$$

$$\boxed{\nu = 4.80 \times 10^{14} \text{ s}^{-1}}$$

- b.) What region of the electromagnetic spectrum is it found?

Visible Region (~400 – 750 nm)

- c.) What is the energy of the wave?

$$E = h\nu = (6.626 \times 10^{-34} \text{ J}\cdot\text{s})(4.80 \times 10^{14} \text{ s}^{-1}) = \boxed{3.18 \times 10^{-19} \text{ J}}$$

- 3.) How many minutes would it take a radio wave to travel from the planet Venus to Earth? (Average distance from Venus to Earth = 28 million miles).

(Note: All electromagnetic travels at the speed of light in a vacuum)

$$2.8 \times 10^7 \text{ mi} \times \frac{1 \text{ km}}{0.6214 \text{ mi}} \times \frac{10^3 \text{ m}}{1 \text{ km}} = 4.5 \times 10^{10} \text{ m}$$

$$4.5 \times 10^{10} \text{ m} \times \frac{1 \text{ s}}{2.998 \times 10^8 \text{ m}} \times \frac{1 \text{ min}}{60 \text{ s}} = \boxed{2.5 \text{ min}}$$

- 4.) The blue color of the sky results from the scattering of sunlight by air molecules. The blue light has a frequency of about $7.5 \times 10^{14} \text{ Hz}$.

- a.) Calculate the wavelength, in nm, associated with this radiation.

$$\lambda = \frac{c}{\nu} = \frac{2.998 \times 10^8 \text{ m}}{7.5 \times 10^{14} \text{ s}^{-1}} \times \frac{1 \text{ nm}}{10^{-9} \text{ m}} = \boxed{4.0 \times 10^2 \text{ nm}} \quad 1 \text{ Hz} = 1 \text{ s}^{-1}$$

- b.) Calculate the energy, in joules, of a single photon associated with this frequency.

$$E = h\nu = (6.626 \times 10^{-34} \text{ J}\cdot\text{s})(7.5 \times 10^{14} \text{ s}^{-1}) = \boxed{5.0 \times 10^{-19} \text{ J}}$$

- 5.) What is ΔE in joules for an atom that releases a photon with a wavelength of 3.2×10^{-7} meters? $\Delta E_{\text{atom}} = E_{\text{photon}} = h\nu = \frac{hc}{\lambda}$

$$\Delta E = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s})(2.998 \times 10^8 \text{ m/s})}{3.2 \times 10^{-7} \text{ m}} = \boxed{6.2 \times 10^{-19} \text{ J}}$$

- 6.) Calculate the frequency (Hz) and wavelength (nm) of the emitted photon when an electron drops from the $n=4$ to $n=2$ state.

$$\Delta E = R_H \left[\frac{1}{n_i^2} - \frac{1}{n_f^2} \right] = (2.179 \times 10^{-18} \text{ J}) \left[\frac{1}{4^2} - \frac{1}{2^2} \right] = \frac{2.179 \times 10^{-18}}{16} - \frac{2.179 \times 10^{-18}}{4}$$

$$= 1.362 \times 10^{-19} - 5.448 \times 10^{-19} = -4.086 \times 10^{-19} \text{ J} = \Delta E$$

$$\Delta E = h\nu$$

$$\nu = \frac{4.086 \times 10^{-19} \text{ J}}{6.626 \times 10^{-34} \text{ J}\cdot\text{s}} = 6.167 \times 10^{14} \text{ Hz} = \nu$$

$$\nu = \frac{\Delta E}{h}$$

$$\lambda = \frac{c}{\nu} = \frac{2.998 \times 10^8 \text{ m/s}}{6.167 \times 10^{14} \text{ s}^{-1}} \times \frac{1 \text{ nm}}{10^{-9} \text{ m}} = \boxed{486.1 \text{ nm}}$$

- 7.) An electron in the hydrogen atom makes a transition from an energy state of principal quantum numbers n_i to the $n = 2$ state. If the photon emitted has a wavelength of 434 nm, what is the value of n_i ?

$$\Delta E_{\text{atom}} = E_{\text{photon}} = h\nu = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s})(2.998 \times 10^8 \text{ m/s})}{434 \times 10^{-9} \text{ m}} = -4.58 \times 10^{-19} \text{ J}$$

(negative number because it is an emission process)

$$\Delta E = R_H \left[\frac{1}{n_i^2} - \frac{1}{n_f^2} \right] = -4.58 \times 10^{-19} \text{ J} = (2.179 \times 10^{-18} \text{ J}) \left[\frac{1}{n_i^2} - \frac{1}{2^2} \right]$$

$$\frac{-4.58 \times 10^{-19} \text{ J}}{2.179 \times 10^{-18} \text{ J}} = \frac{1}{n_i^2} - 0.250 \text{ (keep 3 sf)} \quad -0.210 + 0.250 = \frac{1}{n_i^2} = 0.040$$

$$n_i = \frac{1}{\sqrt{0.040}} \quad \boxed{n_i = 5}$$

- 8.) Protons can be accelerated to speeds near that of light in particle accelerators. Estimate the deBroglie wavelength (in nm) of such a proton moving at 2.90×10^8 m/s. (mass of a proton = 1.673×10^{-27} kg).

$$1 \text{ J} = \frac{1 \text{ kg} \cdot \text{m}^2}{\text{s}^2}$$

$$\lambda = \frac{h}{mu}$$

$$h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s} \times \frac{1 \text{ kg} \cdot \text{m}^2}{\text{s}^2} = 6.626 \times 10^{-34} \frac{\text{kg} \cdot \text{m}^2}{\text{s}}$$

$$\lambda = \frac{6.626 \times 10^{-34} \text{ kg} \cdot \text{m}^2/\text{s}}{(1.673 \times 10^{-27} \text{ kg})(2.90 \times 10^8 \text{ m/s})} = 1.37 \times 10^{-15} \text{ m}$$

$$1.37 \times 10^{-15} \text{ m} \times \frac{1 \text{ nm}}{10^{-9} \text{ m}} = \boxed{1.37 \times 10^{-6} \text{ nm}}$$

9.) Calculate the deBroglie wavelength (in nm) of a 3000. lb automobile traveling at 55 mi/hr.

$$3000. \text{ lb} \times \frac{1 \text{ kg}}{2.2046 \text{ lb}} = 1361 \text{ kg} \qquad \frac{55 \text{ mi}}{1 \text{ hr}} \times \frac{1 \text{ km}}{0.6214 \text{ mi}} \times \frac{10^3 \text{ m}}{1 \text{ km}} \times \frac{1 \text{ hr}}{60 \text{ min}} \times \frac{1 \text{ min}}{60 \text{ sec}} = 25 \frac{\text{m}}{\text{s}}$$

$$\lambda = \frac{h}{mu} = \frac{6.626 \times 10^{-34} \text{ kg} \cdot \text{m}^2/\text{s}}{(1361 \text{ kg})(25 \text{ m/s})} = 1.9 \times 10^{-38} \text{ m} \times \frac{1 \text{ nm}}{10^{-9} \text{ m}} = \boxed{1.9 \times 10^{-29} \text{ nm}}$$

- 14.) The energy required to remove an electron from metal X is $\Delta E = 3.31 \times 10^{-20} \text{ J}$. Calculate the maximum wavelength of light that can photo eject an electron from metal X.

$$E = \frac{hc}{\lambda} \rightarrow \lambda = \frac{hc}{E} = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s})(2.998 \times 10^8 \text{ m/s})}{3.31 \times 10^{-20} \text{ J}}$$

$$\lambda = 6.00 \times 10^{-6} \text{ m} \times \frac{1 \text{ nm}}{10^{-9} \text{ m}} = \boxed{6.00 \times 10^3 \text{ nm}}$$

- 15.) If an electron has a velocity of $5.0 \times 10^5 \text{ m/s}$, what is its wavelength in m?

$$\boxed{\begin{aligned} 1 \text{ J} &= \frac{1 \text{ kg} \cdot \text{m}^2}{\text{s}^2} \\ \lambda &= \frac{h}{mu} \end{aligned}}$$

$$m = \text{mass of electron} = 9.109 \times 10^{-28} \text{ g} \times \frac{1 \text{ kg}}{10^3} = 9.109 \times 10^{-31} \text{ kg}$$

$$h = 6.626 \times 10^{-34} \text{ J}\cdot\text{s} \times \frac{1 \text{ kg} \cdot \text{m}^2}{\text{s}^2} = 6.626 \times 10^{-34} \frac{\text{kg} \cdot \text{m}^2}{\text{s}}$$

$$\lambda = \frac{6.626 \times 10^{-34} \text{ kg} \cdot \text{m}^2/\text{s}}{(9.109 \times 10^{-31} \text{ kg})(5.0 \times 10^5 \text{ m/s})} \quad \boxed{\lambda = 1.5 \times 10^{-9} \text{ m}}$$

- 16.) The laser used to read information from a compact disk has a wavelength of 780 nm. What is the energy associated with one photon of this radiation?

$$E_{\text{photon}} = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s})(2.998 \times 10^8 \text{ m/s})}{780 \times 10^{-9} \text{ nm}} = \boxed{2.55 \times 10^{-19} \text{ J}}$$

- 17.) The retina of a human eye can detect light when radiant energy incident on it is at least $4.0 \times 10^{-17} \text{ J}$. For light of 600 nm wavelength, how many photons does this correspond to?

1.) Determine the energy of 1 photon:

$$E_{\text{photon}} = \frac{hc}{\lambda} = \frac{(6.626 \times 10^{-34} \text{ J}\cdot\text{s})(2.998 \times 10^8 \text{ m/s})}{600 \times 10^{-9} \text{ nm}} = 3.31 \times 10^{-19} \text{ J/photon}$$

2.) Calculate # photons needed to produce given amount of energy:

$$4.0 \times 10^{-17} \text{ J} \times \frac{1 \text{ photon}}{3.31 \times 10^{-19} \text{ J}} = \boxed{1.2 \times 10^2 \text{ photons}}$$